

$$\left. \begin{aligned} \frac{T_0}{T} &= \left(1 + \frac{\gamma-1}{2} M^2\right) \\ \frac{P_0}{p} &= \left(1 + \frac{\gamma-1}{2} M^2\right)^{\frac{\gamma}{\gamma-1}} \end{aligned} \right\} \rightarrow \frac{\dot{m}}{A} = P_0 \sqrt{\frac{2\gamma}{(\gamma-1)(R_g \cdot T_0)} \left[ \left(\frac{p_1}{P_0}\right)^{\frac{2}{\gamma}} - \left(\frac{p_1}{P_0}\right)^{\frac{\gamma+1}{\gamma}} \right]}$$

$$\frac{A_1}{A_2} = \frac{\frac{\dot{m}}{A_2}}{\frac{\dot{m}}{A_1}} = \frac{P_0 \sqrt{\frac{2\gamma}{(\gamma-1)(R_g \cdot T_0)} \left[ \left(\frac{p_2}{P_0}\right)^{\frac{2}{\gamma}} - \left(\frac{p_2}{P_0}\right)^{\frac{\gamma+1}{\gamma}} \right]}}{P_0 \sqrt{\frac{2\gamma}{(\gamma-1)(R_g \cdot T_0)} \left[ \left(\frac{p_1}{P_0}\right)^{\frac{2}{\gamma}} - \left(\frac{p_1}{P_0}\right)^{\frac{\gamma+1}{\gamma}} \right]}} = \frac{\sqrt{\left[ \left(\frac{p_2}{P_0}\right)^{\frac{2}{\gamma}} - \left(\frac{p_2}{P_0}\right)^{\frac{\gamma+1}{\gamma}} \right]}}{\sqrt{\left[ \left(\frac{p_1}{P_0}\right)^{\frac{2}{\gamma}} - \left(\frac{p_1}{P_0}\right)^{\frac{\gamma+1}{\gamma}} \right]}}$$

$$\left(\frac{A_1}{A_2}\right)^2 = \frac{\left[ \left(\frac{p_2}{P_0}\right)^{\frac{2}{\gamma}} - \left(\frac{p_2}{P_0}\right)^{\frac{\gamma+1}{\gamma}} \right]}{\left[ \left(\frac{p_1}{P_0}\right)^{\frac{2}{\gamma}} - \left(\frac{p_1}{P_0}\right)^{\frac{\gamma+1}{\gamma}} \right]} = \frac{P_0^{\frac{2}{\gamma}} \left[ \left(\frac{p_2}{P_0}\right)^{\frac{2}{\gamma}} - \left(\frac{p_2}{P_0}\right)^{\frac{\gamma+1}{\gamma}} \right]}{P_0^{\frac{2}{\gamma}} \left[ \left(\frac{p_1}{P_0}\right)^{\frac{2}{\gamma}} - \left(\frac{p_1}{P_0}\right)^{\frac{\gamma+1}{\gamma}} \right]} = \frac{p_2^{\frac{2}{\gamma}} - \frac{P_0^{\frac{2}{\gamma}}}{P_0^{\frac{\gamma+1}{\gamma}}} \cdot p_2^{\frac{\gamma+1}{\gamma}}}{p_1^{\frac{2}{\gamma}} - \frac{P_0^{\frac{2}{\gamma}}}{P_0^{\frac{\gamma+1}{\gamma}}} \cdot p_1^{\frac{\gamma+1}{\gamma}}} = \frac{p_2^{\frac{2}{\gamma}} - \left(\frac{1}{P_0^{\frac{\gamma-1}{\gamma}}}\right) \cdot p_2^{\frac{\gamma+1}{\gamma}}}{p_1^{\frac{2}{\gamma}} - \left(\frac{1}{P_0^{\frac{\gamma-1}{\gamma}}}\right) \cdot p_1^{\frac{\gamma+1}{\gamma}}}$$

$$\left(\frac{A_1}{A_2}\right)^2 = \frac{\left[ P_0^{\frac{\gamma-1}{\gamma}} \cdot p_2^{\frac{2}{\gamma}} - p_2^{\frac{\gamma+1}{\gamma}} \right]}{\left[ P_0^{\frac{\gamma-1}{\gamma}} \cdot p_1^{\frac{2}{\gamma}} - p_1^{\frac{\gamma+1}{\gamma}} \right]} \rightarrow A_1^2 \cdot \left[ P_0^{\frac{\gamma-1}{\gamma}} \cdot p_1^{\frac{2}{\gamma}} - p_1^{\frac{\gamma+1}{\gamma}} \right] = A_2^2 \cdot \left[ P_0^{\frac{\gamma-1}{\gamma}} \cdot p_2^{\frac{2}{\gamma}} - p_2^{\frac{\gamma+1}{\gamma}} \right]$$

$$A_1^2 \cdot P_0^{\frac{\gamma-1}{\gamma}} \cdot p_1^{\frac{2}{\gamma}} - A_2^2 \cdot P_0^{\frac{\gamma-1}{\gamma}} \cdot p_2^{\frac{2}{\gamma}} = A_1^2 \cdot p_1^{\frac{\gamma+1}{\gamma}} - A_2^2 \cdot p_2^{\frac{\gamma+1}{\gamma}} \rightarrow P_0^{\frac{\gamma-1}{\gamma}} \left( A_1^2 \cdot p_1^{\frac{2}{\gamma}} - A_2^2 \cdot p_2^{\frac{2}{\gamma}} \right) = A_1^2 \cdot p_1^{\frac{\gamma+1}{\gamma}} - A_2^2 \cdot p_2^{\frac{\gamma+1}{\gamma}}$$

$$P_0^{\frac{\gamma-1}{\gamma}} = \frac{A_1^2 \cdot p_1^{\frac{\gamma+1}{\gamma}} - A_2^2 \cdot p_2^{\frac{\gamma+1}{\gamma}}}{A_1^2 \cdot p_1^{\frac{2}{\gamma}} - A_2^2 \cdot p_2^{\frac{2}{\gamma}}} \rightarrow P_0 = \left( \frac{A_1^2 \cdot p_1^{\frac{\gamma+1}{\gamma}} - A_2^2 \cdot p_2^{\frac{\gamma+1}{\gamma}}}{A_1^2 \cdot p_1^{\frac{2}{\gamma}} - A_2^2 \cdot p_2^{\frac{2}{\gamma}}} \right)^{\frac{\gamma}{\gamma-1}} = \left[ \frac{\left(\frac{A_1}{A_2}\right)^2 \cdot (p_1)^{\frac{\gamma+1}{\gamma}} - (p_2)^{\frac{\gamma+1}{\gamma}}}{\left(\frac{A_1}{A_2}\right)^2 \cdot (p_1)^{\frac{2}{\gamma}} - (p_2)^{\frac{2}{\gamma}}} \right]^{\frac{\gamma}{\gamma-1}}$$